# BISON Users Manual

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Fuels Modeling and Simulation Department Idaho National Laboratory

# **BISON Users Manual**

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# **1** Introduction

BISON [1] is a finite element-based nuclear fuel performance code applicable to a variety of fuel forms including light water reactor fuel rods, TRISO particle fuel [2], and metallic rod [3] and plate fuel. It solves the fully-coupled equations of thermomechanics and species diffusion, for 1D spherically symmetric, 2D axisymmetric or 3D geometries. Fuel models are included to describe temperature and burnup dependent thermal properties, fission product swelling, densification, thermal and irradiation creep, fracture, and fission gas production and release. Plasticity, irradiation growth, and thermal and irradiation creep models are implemented for clad materials. Models are also available to simulate gap heat transfer, mechanical contact, and the evolution of the gap/plenum pressure with plenum volume, gas temperature, and fission gas addition. BI-SON is based on the MOOSE framework [4] and can therefore efficiently solve problems using standard workstations or very large high-performance computers.

Two input files are required as input when running BISON. One is a mesh file. While MOOSE supports several file formats, the ExodusII [5] format is the one used almost exclusively in BISON. This file commonly has "e" as its file extension. The mesh file may be generated using CUBIT [6] or another meshing tool. A further option is a meshing script bundled with BISON. This script, dependent on CUBIT and suitable for LWR fuel rod meshes, is the subject of Chapter 22.

The second file is a text file. This file commonly has "i" as its extension and contains a description of the variables, equations, boundary conditions, and material models associated with an analysis. The structure of the text input file is the main focus of this document.

# 2 Running BISON

### 2.1 Checking Out the Code

To checkout the code (for INL onsite users):

```
cd ~/projects
svn co https://hpcsc.inl.gov/svn/herd/trunk
```

For offsite users:

```
cd ~/projects
```

```
svn co https://localhost:4443/svn/herd/trunk
```

It is necessary to build libmesh before building any application.

```
cd ~/projects/trunk/libmesh
./build_libmesh_moose.sh
```

Once libmesh has compiled successfully, you may now compile BISON.

```
cd ~/projects/trunk/bison/
make (add -jn to run on multiple "n" processors)
```

Once BISON has compiled successfully, it is recommended to run the tests to make sure the version of the code you have is running correctly.

```
cd ~/projects/trunk/bison/
./run_test (add -jn to run "n" jobs at one time)
```

### 2.2 Executing BISON

When first starting out with BISON, it is recommended to start from an example problem similar to the problem that you are trying to solve. Multiple examples can be found at bison/examples/ and bison/assessment/. It may be worth running the example problems to see how the code works and modifying input parameters to see how the run time, results and convergence behavior change.

To demonstrate running BISON, consider the input Smeared.i example problem.

```
cd ~/projects/trunk/bison/examples/2D-RZ_rodlet_10pellets
# To run with one processor
~/projects/trunk/bison/bison-opt -i inputSmeared.i
# To run in parallel (4 processors)
mpiexec -n 4 ../../bison-opt -i inputSmeared.i
```

### 2.3 Getting Started

#### 2.3.1 Input to BISON

Before running any problem, the power function, axial profile, mesh, and any functions needed for boundary conditions need to be generated.

Typically, a PiecewiseLinearFile function is used to specify a complex power history. This file has time and power specified in columns or rows, with the first row (or column) being the time (seconds) and the second row (or column) being power (W/m). Any data file that is used as input to BISON must be in Windows comma separated values (csv) format. Looking at inputSmeared.i, the power history is specified as:

```
[./power_history]
type = PiecewiselinearFile
yourFileName = powerhistory.csv
format = rows
scale_factor = 1.0
[../]
```

The axial power profile, if present, is input as a PiecewiseBilinearFile. The axial peaking factors are input as a table within the file, with the top row being the axial location from the bottom of the rod and the left column as time. The axial peaking factors used for the example problem inputSmeared.i for the first three axial locations is as follows:

```
9.44E-03, 1.54E-02, 2.13E-02
0.00E+00, 0.00E+00, 0.00E+00, 0.00E+00
1.00E+00, 5.37E-01, 8.68E-01, 1.01E+00
1.50E+08, 5.37E-01, 8.68E-01, 1.01E+00
```

The mesh can either be generated with the mesh script described in Chapter 22, or if you do not have CUBIT, you can generate a simple 2D-RZ axisymmetric mesh with smeared solid fuel pellets (single fuel column) with the SmearedPelletMesh within BISON. To generate the mesh similar to the one used in the example problem inputSmeared.i, the mesh block would look like:

```
[Mesh]
  type = SmearedPelletMesh
  clad_mesh_density = customize
  pellet_mesh_density = customize
  ny_p = 80 # Total number of axial elements in fuel
  nx_p = 11 # Number of radial elements in fuel
  nx_c = 5 # Number of elements through thickness of clad
  ny_cu = 3 # Number of axial element of upper clad gap
  ny_c = 80 # Number of axial elements of clad wall
  ny_cl = 3 # Number of axial elements of lower clad cap
  clad_thickness = 5.6e-4
  pellet_outer_radius = 0.0041
  clad_bot_height = 1.0e-3
  pellet_quantity = 10
  pellet_height = 0.01186
  plenum_fuel_ratio = 0.045
```

```
clad_gap_width = 8e-5
to_bot_clad_height = 2.24e-3
elem_type = QUAD8
displacements = 'disp_x disp_y'
patch_size = 1000
```

#### 2.3.2 Post Processing

BISON typically writes solution data to an ExodusII file. Data may also be written in other formats, a simple comma separated file giving global data being the most common.

Several options exist for viewing ExodusII results files. These include commercial as well as open-source tools. One good choice is Paraview, which is open-source.

Paraview is available on a variety of platforms. It is capable of displaying node and element data in several ways. It will also produce line plots of global data or data from a particular node or element. A complete description of Paraview is not possible here, but a quick overview of using Paraview with BISON results is available in the BISON workshop material.

#### 2.3.3 Graphical User Interface

It is worth noting that a graphical user interface (GUI) exists for all MOOSE-based applications. This GUI is named Peacock and can be accessed by running .../peacock/peacock from the BISON directory. Information about Peacock may be found on the MOOSE wiki page.

Peacock may be used to generate a text input file. It is also capable of submitting the analysis. Finally, it provides basic post processing capabilities.

# **3** Overview

### 3.1 Basic Syntax

The input file used by BISON is broken into sections or blocks identified with square brackets. The type of input block is placed in the opening brackets, and empty brackets mark the end of the block.

```
[BlockName]
  <block lines and subblocks>
[]
```

Each block may have subblocks, which may in turn have subblocks. The Functions block, for example, will have multiple subblocks, each corresponding to a specific function. The line commands in the Functions subblocks will describe the function details.

Subblocks are opened and closed as

```
[./subblock_name]
<line commands>
[../]
```

Note that the name given in the subblocks must be unique when compared with all other subblocks in the current block.

Line commands are given as key/value pairs with an equal sign between them. They specify parameters to be used by the object being described. The key is a string (no whitespace), and the value may be a string, an integer, a real number, or a list of strings, integers, or real numbers. Lists are given in single quotes and are separated by whitespace.

Often subblocks will include a type line command. This line command specifies the particular type of object being described. The object type indicates which line commands are appropriate for describing the object. BISON will give an error message if a line command is given that does not apply for the current object type. An error message will also be given if a line command is repeated within the current block.

In this document, line commands are shown with the keyword, an equal sign, and, in angle brackets, the value. If a default value exists for that line command, it is shown in parentheses.

In the initial description of a block, line commands common to all subblocks will be described. Those line commands are then omitted from the description of the subblocks but are nonetheless valid line commands for those subblocks.

The name of a subblock ([./<name>]) is most often arbitrary. However, the names of subblocks of Variables, AuxVariables, and Postprocessors define the names used for those entities.

#### 3.2 BISON Syntax Page

A complete listing of all input syntax options is available on the MOOSE wiki page. See the link for Input File Syntax.

### 3.3 Units

Because BISON uses several empirical models, BISON input expects SI units. This simplifies model input by eliminating the possibility of one set of units for one model and another set of units for a different model. Any needed unit conversions are done inside BISON.

### 3.4 High-Level Description of a BISON Simulation

The primary purpose of BISON is to solve coupled systems of partial differential equations (PDEs), where the equations represent important physics related to engineering scale nuclear fuel behavior. Fuel simulations typically consist of solving the following energy, momentum, and mass (or species) conservation equations,

$$\rho C_p \frac{\partial T}{\partial t} + \nabla \cdot \mathbf{q} - e_f \dot{F} = 0, \qquad (3.1)$$

$$\nabla \cdot \boldsymbol{\sigma} + \rho \mathbf{f} = 0. \tag{3.2}$$

$$\frac{\partial C}{\partial t} + \nabla \cdot \mathbf{J} + \lambda C - S = 0, \qquad (3.3)$$

In Equation 3.1, T,  $\rho$  and  $C_p$  are the temperature, density and specific heat, respectively,  $e_f$  is the energy released in a single fission event, and  $\dot{F}$  is the volumetric fission rate.

Momentum conservation (Equation 3.2) is prescribed assuming static equilibrium at each time increment where  $\sigma$  is the Cauchy stress tensor and **f** is the body force per unit mass (e.g. gravity). The displacement field *u*, which is the primary solution variable, is connected to the stress field via the strain, through a constitutive relation.

In the equation for species conservation (3.3) C,  $\lambda$ , and S are the concentration, radioactive decay constant, and source rate of a given species, respectively.

Often, fuels performance problems are limited to thermomechanics, where only Equations 3.1 and 3.2 are solved.

Each term in Equations 3.1 - 3.3 (time derivatives, divergence, source, sinks, etc.) are referred to as kernels and are discussed in greater detail in Chapter 14.

These equations are solved simultaneously using the finite element method (FEM) and JFNK approach [7] on a discretized domain. The domain (also referred to as a mesh) may represent uranium dioxide fuel pellets and zirconium clad in a light water reactor (LWR) simulation. Blocks, side sets, and node sets are defined on the mesh such that material models and boundary conditions can be assigned to different parts of the model. Details regarding the mesh, material models, and boundary conditions can be found in chapters 6, 15, and 10 respectively.

Kernels, boundary conditions, and material models may require supporting information and calculations. This is achieved through the use of Functions and AuxKernels, which are detailed in chapters 9 and 12. For example, a function can be used to define power and time value pairs, which would inform the source term in the energy equation (Equation 3.1). An AuxKernel could be used to define fission rate or burnup, which could be used to inform material models that are dependent on those values. AuxKernels can also be used for writing information, such as stress components, to the output file.

Execution on the analysis is described in the Executioner block. Line commands describe time stepping details and solver options. See Chapter 17 for details.

MOOSE Postprocessors compute a single scalar value at each timestep. These can be minimums, maximums, averages, volumes, or any other scalar quantity. One example of the use of Postprocessors in BISON is computing the gas volume of an LWR rod. The gas volume changes timestep to timestep, but since it is a single scalar quantity, a Postprocessor computes this value. Chapter 16 gives examples.

The following sections delve deeper into the topics mentioned here. The format basically follows that of a typical BISON LWR input file and provides details for each section.

# **4 Global Parameters**

```
[GlobalParams]
order = FIRST
family = LAGRANGE
[]
```

The GlobalParams block specifies parameters that are available, as appropriate, in any other block or subblock in the input file. For example, imagine a subblock that accepts a line command with the keyword value. If the subblock has a line command for value, that line command will be used regardless of what is in GlobalParams. However, if the line command is missing in the subblock but defined in GlobalParams, the subblock will use the parameter defined in GlobalParams. In the example above, the line commands order = FIRST and family = LAGRANGE will be available in all blocks and subblocks in the remainder of the input file.

# 5 Problem

```
[Problem]
  coord_type = <string>
[]
```

The Problem block is typically only used to indicate that a model should run as axisymmetric (RZ) or spherically symmetric (RSPHERICAL). If the model is 3D, the Problem block may be omitted.

# 6 Mesh

```
[Mesh]
file = <string>
displacements = <string list>
patch_size = <integer>
[]
```

```
fileMesh file name. BISON uses ExodusII mesh files.displacementsList of the displacement variables. This line must be given if the analysis<br/>is to use contact or nonlinear geometry. Typically 'disp_x disp_y' for<br/>an axisymmetric analysis.patch_sizeNumber of nearby elements to consider as possible contacting surfaces. A<br/>typical value is 1000.
```

The Mesh block's purpose is to give details about the finite element mesh to be used.

# 7 Variables

```
[Variables]
[./var1]
order = <string>
family = <string>
[../]
[./var2]
order = <string>
family = <string>
initial_condition = <real>
scaling = <real> (1)
[../]
```

order	The order of the variable. Typical values are FIRST and SECOND.
family	The finite element shape function family. A typical value is LAGRANGE.
initial_condition	Optional initial value to be assigned to the variable. Zero is assigned if this line is not present.
scaling	Amount to scale the variable during the solution process. This scal- ing affects only the residual and preconditioning steps and not the final solution values. This line command is sometimes helpful when solving coupled systems where one variable's residual is orders of magnitude different that the other variables' residuals.

The Variables block is where all of the primary solution variables are identified. The name of each variable is taken as the name of the subblocks. Primary solution variables often include temperature (usually named temp) and displacement (usually named disp\_x, disp\_y, and disp\_z).

# 8 AuxVariables

```
[AuxVariables]
[./var1]
order = <string>
family = <string>
[../]
[./var2]
order = <string>
family = <string>
initial_condition = <real>
[../]
```

order	The order of the variable. Typical values are $\ensuremath{\texttt{CONSTANT}}, \ensuremath{\texttt{FIRST}}, \ensuremath{\text{and}}$
	SECOND.
family	The finite element shape function family. Typical values are
	MONOMIAL and LAGRANGE.
initial_condition	Optional initial value to be assigned to the variable. Zero is assigned
	if this line is not present.

The AuxVariables block is where all of the auxiliary variables are identified. The name of each variable is taken as the name of the subblocks. Auxiliary variables are used for quantities such as fast neutron flux, element-averaged stresses, and other output variables.

# 9 Functions

### 9.1 ParsedFunction

```
[./parsedfunction]
type = ParsedFunction
value = <string>
vals = <real list>
vars = <string list>
[../]
```

type ParsedFunction

value String describing the function.

vals Values to be associated with variables in vars.

vars Variable names to be associated with values in vals.

The ParsedFunction function takes a mathematical expression in value. The expression can be a function of time (t) or coordinate (x, y, or z). The expression can include common mathematical functions. Examples include '4e4+1e2\*t', 'sqrt(x\*x+y\*y+z\*z)', and 'if(t<=1.0, 0.1\*t, (1.0+0.1)\*cos(pi/2\*(t-1.0)) - 1.0)'. Constant variables may be used in the expression if they have been declared with vars and defined with vals. Further information can be found at http://warp.povusers.org/FunctionParser/.

### 9.2 PiecewiseLinear

```
[./piecewiselinear]
type = PiecewiseLinear
x = <real list>
y = <real list>
scale_factor = <real> (1.0)
axis = <0, 1, or 2 for x, y, or z>
[../]
```

type	PiecewiseLinear
Х	List of x values for x-y data.
У	List of y values for x-y data.
scale_factor	Scale factor to be applied to resulting function. Default is 1

axis Coordinate direction to use in the function evaluation. If not present, time is used as the function input.

The PiecewiseLinear function takes pairs of x-y data as input and interpolates values based on those pairs. By default, the x-data corresponds to time, but this can be changed to correspond to x, y, or z coordinate with the axis line. If the function is queried outside of its range of x data, it returns the y value associated with the closest x data point.

### 9.3 PiecewiseBilinear

```
[./piecewiselinear]
type = PiecewiseBilinear
yourFileName = <string>
axis = <0, 1, or 2 for x, y, or z>
xaxis = <0, 1, or 2 for x, y, or z>
yaxis = <0, 1, or 2 for x, y, or z>
scale_factor = <real> (1.0)
radial = <bool> (false)
[../]
```

type	PiecewiseBilinear
yourFileName	File holding your csv data.
axis	Coordinate direction to use in the function evaluation.
xaxis	Coordinate direction used for x-axis data.
yaxis	Coordinate direction used for y-axis data.
scale_factor	Scale factor to be applied to resulting function. Default is 1.
radial	Set to true if interpolation should be done along a radius rather than along
	a specific axis. Requires xaxis and yaxis.

The PiecewiseBilinear function reads a csv file and interpolates values based on the data in the file. The interpolation is based on x-y pairs. If axis is given, time is used as the y index. Either xaxis or yaxis or both may be given. Time is used as the other index if one of them is not given. If radius is given, xaxis and yaxis are used to orient a cylindrical coordinate system, and the x-y pair used in the query will be the radial coordinate and time.

### 9.4 Composite

```
[./composite]
type = CompositeFunction
functions = <string list>
scale_factor = <real> (1.0)
[../]
```

type	CompositeFunction
functions	List of functions to be multiplied together.
scale_factor	Scale factor to be applied to resulting function. Default is 1.

The Composite function takes an arbitrary set of functions, provided in the functions parameter, evaluates each of them at the appropriate time and position, and multiplies them together. The function can optionally be multiplied by a scale factor, which specified using the scale\_factor parameter.

# **10 Boundary Conditions**

The BCs block is for specifying various types of boundary conditions.

```
[BCs]
[./name]
type = <BC type>
boundary = <string list>
...
[../]
[]
```

type Type of boundary condition.

boundary List of boundaries (side sets). Either boundary numbers or names.

## **10.1 Dirichlet**

#### 10.1.1 DirichletBC

```
[./dirichletbc]
type = DirichletBC
variable = <variable>
boundary = <string list>
value = <real>
[../]
```

type DirichletBC	
------------------	--

variable	Primary variable associated with this boundary condition.
boundary	List of boundary names or ids where this boundary condition will apply.
value	Value to be assigned.

### 10.1.2 PresetBC

The PresetBC takes the same inputs as DirichletBC and also acts as a Dirichlet boundary condition. However, the implementation is slightly different. PresetBC causes the value of the boundary condition to be applied before the solve begins where DirichletBC enforces the boundary condition as the solve progresses. In certain situations, one is better than another.

### 10.1.3 FunctionDirichletBC

```
[./functiondirichletbc]
type = FunctionDirichletBC
variable = <variable>
boundary = <string list>
function = <string>
[../]
```

type	FunctionDirichletBC
variable	Primary variable associated with this boundary condition.
boundary	List of boundary names or ids where this boundary condition will apply.
function	Function that will give the value to be applied by this boundary condition.

#### 10.1.4 FunctionPresetBC

The FunctionPresetBC takes the same inputs as FunctionDirichletBC and also acts as a Dirichlet boundary condition. However, the implementation is slightly different. FunctionPresetBC causes the value of the boundary condition to be applied before the solve begins where FunctionDirichletBC enforces the boundary condition as the solve progresses. In certain situations, one is better than another.

# 10.2 Pressure

```
[./Pressure]
[./pressure]
boundary = <string list>
factor = <real> (1)
function = <string>
[../]
[../]
```

boundary	List of boundary names or ids where this boundary condition will apply.
factor	Magnitude of pressure to be applied. If function is also given, factor is mul-
	tiplied by the output of the function and then applied as the pressure.
function	Function that will give the value to be applied by this boundary condition.

The Pressure boundary condition uses two levels of nesting within the BCs block. This allows the pressure to be applied properly in all coordinate directions although it is specified one time only.

### 10.3 PlenumPressure

```
[./PlenumPressure]
 [./plenumpressure]
   boundary = <string list>
   initial_pressure = <real> (0)
   startup_time = <real> (0)
   R = <real>
   output_initial_moles = <string>
   temperature = <string>
   volume = <string>
   material_input = <string list>
   output = <string>
   refab_time = <real list>
   refab_pressure = <real list>
   refab_volume = <real list>
   refab_type = <integer list>
 [../]
[../]
```

boundary	List of boundary names or ids where this boundary condition will apply.
initial_pressure	The initial pressure in the plenum.
startup_time	The amount of time during which the pressure will ramp from zero to its true value.
R	The universal gas constant. In BISON, SI units are used, and R should be 8.3143.
output_initial_moles	If given, the reporting Postprocessor to use for the initial moles of gas.
temperature	The name of the Postprocessor holding the average temperature value.
volume	The name of the Postprocessor holding the internal volume.
material_input	The name of the Postprocessors that hold the amount of material injected into the plenum.
output	If given, the reporting Postprocessor to use for the plenum pressure value.
refab_time	The time(s) at which the plenum pressure must be reinitialized (likely due to fuel rod refabrication).
refab_pressure	The pressure of fill gas at refabrication. Number of values must match number in refab_time.
refab_temperature	The temperature at refabrication. Number of values must match number in refab_time.
refab_volume	The gas volume at refabrication. Number of values must match number in refab_time.

The PlenumPressure block is used to specify internal rod pressure as a function of temperature, cavity volume, and moles of gas.

The PlenumPressure boundary condition uses two levels of nesting within the BCs block. This allows the pressure to be applied properly in all coordinate directions although it is specified one time only.

### 10.4 CoolantChannel

```
[CoolantChannel]
  [./coolantchannel]
   boundary = <string list>
   variable = <string>
   axial_power_profile = <string>
   cond_metal = <real>
   cond_oxide = <real>
   coupledEnthalpy = <string>
   direction = <string>
   direction2 = <string>
   flow_area = <real>
   heat_flux = <string>
   heat_transfer_coefficient = <string or real>
   heat_transfer_mode = <string> (0)
   heated_diameter = <real>
   heated_perimeter = <real>
   htc_correlation_type = <string>
   hydraulic_diameter = <real>
   inlet_massflux = <string or real>
   inlet_pressure = <string or real>
   inlet_temperature = <string or real>
   linear_heat_rate = <string>
   number_axial_zone = <integer> (0)
   number_lateral_zone = <integer> (1)
   oxide_thickness = <string>
   oxide_model = <string> (zirconia)
   pbr = <real>
   rod_diameter = <real> (0.01)
   rod_pitch = \langle real \rangle (0.0126)
  [../]
[]
```

boundary
variable
axial\_power\_profile
cond\_metal
cond\_oxide

List of boundaries. Typically only one boundary id is given. Name of variable associated with this BC. Typically temp. Function name for function describing axial power factors. Conductivity of the metal. Used if oxide\_model is user. Conductivity of the oxide. Used if oxide\_model is user.

coupledEnthalpy	Variable name. If given, enthalpy is taken from this variable directly instead of being calculated.
direction	One of x, y, or z. Coordinate direction associated with fluid flow. Default is y.
direction2	One of x, y, or z. Coordinate direction associated with lat- eral dimension of model. Default is x. This input is used for plate geometry.
flow_area	Flow area. If used, must be used with heated_diameter, heated_perimeter, and hydraulic_diameter. If used, rod_diameter and rod_pitch will be ignored.
heat_flux	Function name for function describing the heat flux at the cladding surface.
heat_transfer_coefficient	Either a function name for a function describing the heat transfer coefficient or a real value to be assigned as the heat transfer coefficient. If present, other parameters controlling the heat transfer coefficient calculation will be ignored.
heat_transfer_mode	One of 0 (automatic), 1 (natural convection), 2 (forced liq- uid convection), 3 (subcooled boiling), 4 (saturated boil- ing), or 5 (DNB low flow).
heated_diameter	Heated diameter. If used, must be used with flow_area, heated_perimeter, and hydraulic_diameter. If used, rod_diameter and rod_pitch will be ignored.
heated_perimeter	Heated perimeter. If used, must be used with flow_area, heated_diameter, and hydraulic_diameter. If used, rod_diameter and rod_pitch will be ignored.
htc_correlation_type	One of 1 (Thom), 2 (Jens Lottes), 3 (Chen), 4 (Shrock-Grossman), or 5 (constant).
hydraulic_diameter	Hydraulic diameter. If used, must be used with flow_area, heated_perimeter, and heated_diameter. If used, rod_diameter and rod_pitch will be ignored.
inlet_massflux	Either a function name for a function describing the inlet mass flux or a real value to be assigned as the inlet mass flux.
inlet_pressure	Either a function name for a function describing the inlet pressure or a real value to be assigned as the inlet pressure.
inlet_temperature	Either a function name for a function describing the inlet temperature or a real value to be assigned as the inlet tem- perature.
linear_heat_rate	Function name for a function describing the linear heat rate.

number_axial_zone	Number of axial divisions along the cladding to be used in integrating the heat flux.
number_lateral_zone	Number of lateral divisions along the cladding to be used in integrating the heat flux. This input is used for plate geometry.
oxide_thickness	Name of AuxVariable representing the oxide thickness. If not given, the calculated heat transfer coefficient will not account for an oxide layer.
oxide_model	One of zirconia, alumina, or user.
rod_diameter	Diameter of the fuel rod.
rod_pitch	Pitch or spacing between fuel rods.

The effect of the coolant on the heat transfer at the exterior cladding surface can be modeled using the CoolantChannel feature. This feature appears in the input file in its own block (i.e., not inside the BCs block).

The presence of some input parameters causes others to be ignored. The following describes the input parameter precedence.

If heat\_transfer\_coefficient is given, its value will be assigned to the given boundary. All other parameters related to the heat transfer coefficient calculation are ignored.

Enthalpy is taken as coupledEnthalpy if present. Otherwise, heat flux is calculated based on linear\_heat\_rate, specification of number\_axial\_zone, and specification of heat\_flux, in highest precedence order. The integrated heat flux is computed based on the same precedence. As an example, if number\_axial\_zone and heat\_flux are specified, heat\_flux will be ignored. These are used as inputs to the heat transfer coefficient correlations.

# **11 Contact**

Finite element contact enforces constraints between surfaces in the mesh. Mechanical contact prevents penetration and develops contact forces. Thermal contact transfers heat between the surfaces.

### **11.1 Mechanical Contact**

```
[Contact]
 [./contact]
   disp_x = <variable>
   disp_y = <variable>
   disp_z = <variable>
   formulation = <string> (DEFAULT)
   friction_coefficient = <real> (0)
   master = <string>
   model = <string> (frictionless)
   normal_smoothing_distance = <real>
   normal_smoothing_method = <string> (edge_based)
   order = <string> (FIRST)
   penalty = <real> (1e8)
   slave = <string>
   tangential_tolerance = <real>
   tension_release = <real>
 [../]
[]
```

disp_x	Variable name for displacement variable in x direction. Typically disp_x.
disp_y	Variable name for displacement variable in y direction. Typically ${\tt disp\_y}.$
disp_z	Variable name for displacement variable in z direction. Typically ${\tt disp_z}.$
formulation	One of DEFAULT or PENALTY.
friction_coefficient	The friction coefficient.
master	The boundary id for the master surface.
model	One of frictionless, glued, or coulomb.

normal_smoothing_distance	Distance from face edge in parametric coordinates over which to smooth the contact normal. 0.1 is a reasonable value.
normal_smoothing_method	One of edge_based or nodal_normal_based. If
	nodal_normal_based, must also have a NodalNormals
	block.
order	The order of the variable. Typical values are FIRST and
	SECOND.
penalty	The penalty stiffness value to be used in the constraint.
slave	The boundary id for the slave surface.
tangential_tolerance	Tangential distance to extend edges of contact surfaces.
tension_release	Tension release threshold. A node will not be released if its tensile load is below this value. Must be positive.

In LWR fuel analysis, the cladding surface is typically the master surface, and the fuel surface is the slave surface. It is good practice to make the master surface the coarser of the two.

The robustness and accuracy of the mechanical contact algorithm is strongly dependent on the penalty parameter. If the parameter is too small, inaccurate solutions are more likely. If the parameter is too large, the solver may struggle.

The DEFAULT option uses an enforcement algorithm that moves the internal forces at a slave node to the master face. The distance between the slave node and the master face is penalized. The PENALTY algorithm is the traditional penalty enforcement technique.

### **11.2 Thermal Contact**

#### 11.2.1 GapHeatTransfer

```
[ThermalContact]
 [./thermalcontact]
   type = GapHeatTransfer
   disp_x = <variable>
   disp_y = <variable>
   disp_z = <variable>
   emissivity_1 = <real> (0)
   emissivity_2 = <real> (0)
   gap_conductivity = <real> (1)
   gap_conductivity_function = <string>
   gap_conductivity_function_variable = <string>
   master = <string>
   min_gap = <real> (1e-6)
   max_gap = < real > (1e6)
   normal_smoothing_distance = <real>
   normal_smoothing_method = <string> (edge_based)
   order = <string> (FIRST)
```

```
quadrature = <bool> (false)
slave = <string>
stefan_boltzmann = <real> (5.669e-8)
variable = <string>
[../]
```

type	GapHeatTransfer
disp_x	Variable name for displacement variable in x di- rection. Typically disp_x. Optional.
disp_y	Variable name for displacement variable in y di- rection. Typically disp_y. Optional.
disp_z	Variable name for displacement variable in z di- rection. Typically disp_z. Optional.
emissivity_1	The emissivity of the fuel surface.
emissivity_2	The emissivity of the cladding surface.
gap_conductivity	The thermal conductivity of the gap material.
gap_conductivity_function	Thermal conductivity of the gap material as a function. Multiplied by gap_conductivity.
gap_conductivity_function_variable	Variable to be used in thermal_conductivity_function in place of time.
master	The boundary id for the master surface.
min_gap	The minimum permissible gap size.
max_gap	The maximum permissible gap size.
normal_smoothing_distance	Distance from face edge in parametric coordi- nates over which to smooth the contact normal. 0.1 is a reasonable value.
normal_smoothing_method	One of edge_based or nodal_normal_based. If nodal_normal_based, must also have a NodalNormals block.
order	The order of the variable. Typical values are FIRST and SECOND.
quadrature	Whether or not to use quadrature point-based gap heat transfer.
slave	The boundary id for the slave surface.
stefan_boltzmann	The Stefan-Boltzmann constant.
tangential_tolerance	Tangential distance to extend edges of contact surfaces.

The quadrature option is recommended with second-order meshes.

#### 11.2.2 GapHeatTransferLWR

```
[ThermalContact]
  [./thermalcontact]
   type = GapHeatTransferLWR
   contact_coef = <real> (10)
   contact_pressure = <string>
   disp_x = <variable>
   disp_y = <variable>
   disp_z = <variable>
   emissivity_1 = <real> (0)
   emissivity_2 = <real> (0)
   external_pressure = <real> (0)
   initial_gas_fractions = <real list> (1 0 0 0 0 0 0 0 0)
   initial_moles = <string>
   gas_released = <string list>
   gas_released_fractions = <real list> (0 0 0.153 0.847 0 0 0 0 0 0)
   jump_distance_fuel = <real> (0)
   jump_distance_clad = <real> (0)
    jump_distance_model = <string> (DIRECT)
   master = <string>
   meyer_hardness <real> (0.68e9)
   min_gap = <real> (1e-6)
   max_gap = < real > (1e6)
   normal_smoothing_distance = <real>
   normal_smoothing_method = <string> (edge_based)
   order = <string> (FIRST)
   quadrature = <bool> (false)
   refab_gas_fractions = <real list>
   refab_time = <real list>
   refab_type = <integer list>
   roughness_fuel = <real> (1e-6)
   roughness_clad = <real> (1e-6)
   roughness_coef = <real> (1.5)
   slave = <string>
   stefan_boltzmann = <real> (5.669e-8)
   variable = <string>
  [../]
[]
```

type	GapHeatTransferLWR
contact_coef	The leading coefficient on the solid-solid conduction relation $(1/\sqrt{m})$ .
contact_pressure	The contact pressure variable. Typically contact_pressure.
disp_x	Variable name for displacement variable in x direction. Typically disp_x. Optional.

disp_y	Variable name for displacement variable in y direction. Typically disp_y. Optional.
disp_z	Variable name for displacement variable in z direction. Typically disp_z. Optional.
emissivity_1	The emissivity of the fuel surface.
emissivity_2	The emissivity of the cladding surface.
external_pressure	The external (gas) pressure.
initial_gas_fractions	The initial fractions of constituent gases (helium, ar- gon, krypton, xenon, hydrogen, nitrogen, oxygen, carbon monoxide, carbon dioxide, water vapor).
initial_moles	The Postprocessor that will give the initial moles of gas.
gas_released	List of one or more Postprocessors that give the gas re- leased.
gas_released_fractions	The fraction of released gas that is assigned to helium, ar- gon, krypton, xenon, hydrogen, nitrogen, oxygen, carbon monoxide, carbon dioxide, and water vapor. One set of fractions for each Postprocessor listed in gas_released.
jump_distance_fuel	The temperature jump distance of the fuel.
jump_distance_clad	The temperature jump distance of the clad.
jump_distance_model	One of DIRECT (specify distances directly) or KENNARD (jump distances computed based on gas properties).
master	The boundary id for the master surface.
meyer_hardness	The Meyer hardness of the softer material (Pa).
min_gap	The minimum permissible gap size.
max_gap	The maximum permissible gap size.
normal_smoothing_distance	Distance from face edge in parametric coordinates over which to smooth the contact normal. 0.1 is a reasonable value.
normal_smoothing_method	One of edge_based or nodal_normal_based. If nodal_normal_based, must also have a NodalNormals block.
order	The order of the variable. Typical values are FIRST and SECOND.
plenum_pressure	The name of the plenum pressure Postprocessor.
quadrature	Whether or not to use quadrature point-based gap heat transfer.
refab_gas_fractions	The fractions of constituent gases at refabrication (helium, argon, krypton, xenon, hydrogen, nitrogen, oxygen, carbon monoxide, carbon dioxide, water vapor).

refab_time	The time(s) at which refabrication occurs. If multiple times are given, multiple sets of refab_gas_fractions and multiple refab_types must be given.
refab_type	One of 0 (instantaneous reset, evolving gas fraction there- after) or 1 (instantaneous reset, constant gas fraction there- after).
roughness_fuel	The roughness of the fuel surface.
roughness_clad	The roughness of the cladding surface.
roughness_coef	The coefficient for the roughness summation.
slave	The boundary id for the slave surface.
stefan_boltzmann	The Stefan-Boltzmann constant.
tangential_tolerance	Tangential distance to extend edges of contact surfaces.

GapHeatTransferLWR differs from GapHeatTransfer in that the gap conductivity is computed based on the gases in the gap. To this may also be added the effect of solid-solid conduction. The gas in the gap may be flushed in a refabrication step. (See also PlenumPressure (10.3).)

The quadrature option is recommended with second-order meshes.

# 12 AuxKernels and AuxBCs

AuxKernels and AuxBCs are used to compute values for AuxVariables. They often compute quantities based on functions, solution variables, and material properties.

```
[AuxKernels]
[./name]
type = <AuxKernel type>
block = <string list>
...
[../]
[]
[AuxBCs]
[./name]
type = <AuxBC type>
boundary = <string list>
...
[../]
[]
```

type	Type of auxiliary kernel.
block	List of blocks. Either block numbers or names.
boundary	List of boundaries (side sets). Either boundary numbers or names.

All AuxKernels act on blocks. All AuxBCs act on boundaries. If no block or boundary is specified, the AuxKernel or AuxBC will act on the entire model.

Note that the same types are recognized in AuxKernels and AuxBCs.

### 12.1 AuxKernels for Output

#### 12.1.1 MaterialTensorAux

```
[./materialtensoraux]
type = MaterialTensorAux
tensor = <material property tensor>
variable = <variable>
index = <integer>
quantity = <string>
point1 = <vector> (0, 0, 0)
point2 = <vector> (0, 1, 0)
```

type	MaterialTensorAux
tensor	Name of second-order tensor material property. A typical second-order tensor material property is ${\tt stress}.$
variable	Name of AuxVariable that will hold result.
index	Index into tensor, from 0 to 5 (xx, yy, zz, xy, yz, zx). Either index or quantity must be specified
	must be specified.
quantity	One of VonMises, PlasticStrainMag, Hydrostatic, Hoop, Radial,
	Axial, MaxPrincipal, MedPrincipal, MinPrincipal, FirstInvariant,
	SecondInvariant, ThirdInvariant, or TriAxiality. Either index or
	quantity <b>must be specified</b> .

The MaterialTensorAux AuxKernel is used to output quantities related to second-order tensors used as material properties. Stress and strain are common examples of these tensors. The AuxKernel allows output of specific tensor entries or quantities computed from the entire tensor. Typically, the AuxVariable computed by MaterialTensorAux will be an element-level, constant variable. The computed value will be the volume-averaged quantity over the element.

#### 12.1.2 MaterialRealAux

```
[./materialrealaux]
type = MaterialRealAux
property = <material property>
variable = <variable>
[../]
```

### type MaterialRealAux

tensor Name of material property.

variable Name of AuxVariable that will hold result.

The MaterialRealAux AuxKernel is used to output material properties. Typically, the Aux-Variable computed by MaterialTensorAux will be an element-level, constant variable. The computed value will be the volume-averaged quantity over the element.

### 12.2 AuxKernels for Specifying Fission Rate

Note that these AuxKernels are not needed if the Burnup block (see Chapter 13) is present.

#### 12.2.1 FissionRateAuxLWR

```
[./fissionrateauxlwr}
type = FissionRateAuxLWR
value = <real> (1)
function1 = <string>
function2 = <string>
pellet_diameter = <real> (0.0082)
pellet_inner_diameter = <real> (0)
fuel_volume_ratio = <real> (1)
energy_per_fission = <real> (3.28451e-11)
[../]
```

value	Fission rate if function1 is not present. Scale factor if function1 is given.
function1	Function describing rod averaged linear power. This power is the total power, the power from the volumetric fission rate times the volume of fuel times the energy per fission.
function2	Function describing axial power profile.
pellet_diameter	The diameter of the fuel.
pellet_inner_diameter	The inner diameter of the fuel.
fuel_volume_ratio	Reduction factor for deviation from right circular cylinder fuel. The ratio of actual volume to right circular cylinder volume.
energy_per_fission	The energy released per fission in J/fission.

FissionRateAuxLWR is designed to calculate fission rate given rod averaged linear power and pellet dimensions.

#### 12.2.2 FissionRateAux

```
[./fissionrateaux]
type = FissionRateAux
variable = <string>
block = <string list>
function = <string>
value = <real>
[../]
```

type FissionRateAux

- value Value of fission rate. If function is present, value is multiplied by the function value.
- function Function describing the fission rate.
The FissionRateAux AuxKernel simply sets the value of a variable that stores the fission rate (fissions/ $m^3$ /s) to either a constant value or a value prescribed by a function. If both function and value are provided, value is used as a scaling factor on the function.

#### 12.2.3 FissionRateFromPowerDensity

```
[./fissionratefrompowerdensity]
type = FissionRateFromPowerDensity
variable = <string>
block = <string list>
function = <string>
energy_per_fission = <real>
[../]
```

type	FissionRateAux
variable	Name of AuxVariable that will hold fission rate. Typically fission_rate.
function	Function describing the power density in W/m <sup>3</sup> .
energy_per_fission	Energy released per fission in J/fission.

Like FissionRateAux, the FissionRateFromPowerDensity AuxKernel sets the fission rate based on a function and a scaling factor. This AuxKernel is intended to be used specifically in the case where the input function defines the power density (in W/m<sup>3</sup>). The power density is divided by user-provided constant that defines the energy per fission (J/fission) to provide the fission rate in (fissions/m<sup>3</sup>/s).

## 12.3 Other AuxKernels

#### 12.3.1 Al2O3Aux

```
[./al2o3aux]
type = Al2O3Aux
variable = <string>
function = <string>
model = <string> (function)
temp = <string>
[../]
```

type Al2O3Aux

- variable Variable name corresponding to the Al2O3 thickness.
- function Function describing the Al2O3 thickness as a function of time.
- model One of function or griess. The griess option invokes a correlation appropriate for plate fuel.

temp Variable name for temperature variable. Typically temp.

#### 12.3.2 BurnupAux

```
[./burnupaux]
type = BurnupAux
fission_rate = <string>
density = <real>
molecular_weight = <real> (0.270)
[../]
```

type	BurnupAux		
variable	Variable name corresponding to the burnup. Typically burnup.		
fission_rate	Variable name corresponding to the fission rate. Typically fission_rate.		
density	The initial fuel density.		
molecular_weight	The molecular weight.		

BurnupAux computes burnup given the fission rate. Note that this AuxKernel is not needed if the Burnup block (see Chapter 13) is present.

## 12.3.3 FastNeutronFluxAux

```
[./fastneutronfluxaux]
  type = FastNeutronFluxAux
  variable = <string>
  fast_neutron_flux = <string>
[../]
```

type	FastNeutronFluxAux	
variable	Variable name corresponding to the fast neutron flux. Typically	
	fast_neutron_flux.	
rod_ave_lin_pow	Function describing rod averaged linear power. This power is the total power, the power from the volumetric fission rate times the volume of fuel times the energy per fission.	
axial_power_profile	Function describing axial power profile.	
factor	The fast neutron flux if <code>rod_ave_lin_pow</code> is not given. Otherwise, a scale factor. Recommended scale factor value is 3e13 (n/( $m^2-s$ )/( $W/m$ )).	

#### 12.3.4 FastNeutronFluenceAux

```
[./fastneutronfluenceaux]
type = FastNeutronFluenceAux
variable = <string>
fast_neutron_flux = <string>
[../]
```

type	FastNeutronFluenceAux	
variable	Variable name corresponding to the fast neutron fluence.	Typically
	fast_neutron_fluence.	
fast_neutron_flux	Variable name corresponding to the fast neutron flux.	Typically
	fast_neutron_flux.	

#### 12.3.5 GrainRadiusAux

```
[./grainradiusaux]
type = GrainRadiusAux
variable = <string>
temp = <string>
[../]
```

type GrainRadiusAux

variable Variable name corresponding to the fuel grain radius.

temp Variable name for temperature variable. Typically temp.

The GrainRadiusAux model is a simple empirical model for calculating grain growth. This can be used with the Sifgrs model (15.3.2).

#### 12.3.6 OxideAux

```
[./oxideaux]
type = OxideAux
variable = <string>
fast_neutron_flux = <string>
lithium_concentration = <real> (0)
model_option = <int> (1)
oxide_scale_factor = <real> (1)
tin_content = <real> (1.38)
temp = <string>
use_coolant_channel = <bool> (false)
```

type variable OxideAux Variable name corresponding to the zirconia thickness.

fast_neutron_flux	Variable name corresponding to the fast neutron flux. Typically	
	fast_neutron_flux.	
lithium_concentration	Lithium concentration in ppm.	
model_option	If 1, uses the EPRI KWU CE model. Otherwise, uses the EPRI	
	SLI model.	
oxide_scale_factor	Scale factor applied to the rate of oxide growth.	
tin_content	Tin content in wt%.	
temp	Variable name for temperature variable. Typically temp.	
use_coolant_model	If true, model will adjust surface temperature based on the coolant channel model.	

### 12.3.7 PelletIdAux

```
[./pelletidaux]
type = PelletIdAux
a_lower = <real>
a_upper = <real>
number_pellets = <integer>
[../]
```

type	PelletIdAux
a_lower	The lower axial coordinate of the fuel stack.
a_upper	The upper axial coordinate of the fuel stack.
number_pellets	Number of fuel pellets.

PelletIdAux is used to compute a pellet number. It may be used with a discrete pellet or smeared fuel column mesh.

# 13 Burnup

```
[Burnup]
  [./burnup]
   rod_ave_linear_power = <string>
   axial_power_profile = <string>
   num_radial = <integer>
   num_axial = <integer>
   a_lower = <real>
   a_upper = <real>
   fuel_inner_radius = <real> (0)
   fuel_outer_radius = <real> (0.0041)
   fuel_volume_ratio = <real> (1)
   density = <real>
   energy_per_fission = <real> (3.28451e-11)
   i_enrich = <real list> (0.05, 0.95, 0, 0, 0, 0)
   sigma_c = <real list> (9.7, 0.78, 58.6, 100, 50, 80)
   sigma_f = <real list> (41.5, 0, 105, 0.584, 120, 0.458)
   sigma_a_thermal = <real list> (sum of sigma_c and sigma_f)
   N235 = <string>
   N238 = <string>
   N238 = <string>
   N240 = <string>
   N241 = <string>
   N242 = <string>
   RPF = <string>
  [../]
[]
```

block	List of fuel blocks. Either block numbers or names.	
rod_ave_lin_pow	Function describing rod averaged linear power. This power is the total power, the power from the volumetric fission rate times the volume of fuel times the energy per fission.	
axial_power_profile	Function describing axial power profile.	
num_radial	Number of radial divisions in secondary grid used to compute ra- dial power profile.	
num_axial	Number of axial divisions in secondary grid used to compute radial power profile.	
a_lower	The lower axial coordinate of the fuel stack.	
a_upper	The upper axial coordinate of the fuel stack.	

fuel_inner_radius	The inner radius of the fuel.		
fuel_outer_radius	The outer radius of the fuel.		
fuel_volume_ratio	Reduction factor for deviation from right circular cylinder fuel. The ratio of actual volume to right circular cylinder volume.		
density	The initial fuel density.		
energy_per_fission	The energy released per fission in J/fission.		
i_enrich	The initial enrichment for the six isotopes.		
sigma_c	The capture cross sections for the six isotopes.		
sigma_f	The fission cross sections for the six isotopes.		
sigma_a_thermal	The absorption (thermal) cross sections for the six isotopes.		
N235	Indicates that the output of the concentration of N235 is required. Typically N235.		
N238	Indicates that the output of the concentration of N238 is required. Typically N238.		
N239	Indicates that the output of the concentration of N239 is required. Typically N239.		
N240	Indicates that the output of the concentration of N240 is required. Typically N240.		
N241	Indicates that the output of the concentration of N241 is required. Typically N241.		
N242	Indicates that the output of the concentration of N242 is required. Typically N242.		
RPF	Indicates that the output of the radial power factor is required. Typ- ically RPF.		

The Burnup block computes fission rate and burnup for LWR fuel including the radial power factor. It is not appropriate for other fuel configurations. Use of the Burnup block will cause BISON to create and populate burnup, fission\_rate, and optionally other AuxVariables.

The radial power factor calculation is performed on a secondary numerical grid, created internally by BISON. This is the reason for the num\_radial and num\_axial line commands. Once the fission rate, burnup, and other quantities are computed on this secondary grid, they are mapped back to the finite element mesh.

# 14 Kernels

Kernels are used to volume integrals associated with a given term in a PDE. They often compute quantities based on functions, solution variables, auxiliary variables, and material properties.

```
[Kernels]
 [./name]
 type = <kernel type>
 block = <string list>
 ...
[../]
[]
```

type Type of kernel.

block List of blocks. Either block numbers or names.

All Kernels act on blocks. If no block is specified, the Kernel will act on the entire model.

## 14.1 SolidMechanics

```
[SolidMechanics]
 [./solidmechanics]
 disp_x = <variable>
 disp_y = <variable>
 disp_z = <variable>
 disp_r = <variable>
 temp = <variable>
[../]
```

- disp\_x Variable name for displacement variable in x direction. Typically disp\_x.
- disp\_y Variable name for displacement variable in y direction. Typically disp\_y.
- disp\_z Variable name for displacement variable in z direction. Typically disp\_z for 3D and disp\_y for axisymmetric models.
- disp\_r Variable name for displacement variable in radial direction for axisymmetric or spherically symmetric cases. Typically disp\_x.
- temp Variable name for temperature variable. Necessary for thermal expansion. Typically temp.

The SolidMechanics block specifies inputs for the divergence of stress as part of the equations of solid mechanics. The divergence of stress is a Kernel in MOOSE nomenclature. The SolidMechanics block informs MOOSE of the divergence kernels but is not placed inside the Kernels block in the input file.

### 14.2 Gravity

```
[./gravity]
  type = Gravity
  variable = <variable>
  value = <real>
[../]
```

type	Gravity
variable	Variable name corresponding to the displacement direction in which the gravity load should be applied.
value	Acceleration of gravity. Typically -9.81 (m/s <sup>2</sup> ).

Gravity may be applied to the model with this kernel. The required density is computed and provided internally given inputs in the Materials block.

## 14.3 Heat Conduction

```
[./heatconduction]
type = HeatConduction
variable = <variable>
[../]
```

type HeatConduction

variable Variable name corresponding to the heat conduction equation. Typically temp.

Kernel for diffusion of heat or divergence of heat flux.

## 14.4 Heat Conduction Time Derivative

```
[./heatconductiontimederivative]
  type = HeatConductionTimeDerivative
  variable = <variable>
[../]
```

type HeatConductionTimeDerivative

variable Variable name corresponding to the heat conduction equation. Typically temp.

Kernel for  $\rho C_p \partial T / \partial t$  term of the heat equation.

# 14.5 Neutron Heat Source

```
[./neutronheatsource]
  type = NeutronHeatSource
  variable = <variable>
  fission_rate = <variable>
[../]
```

type	NeutronHeatSource
variable	Variable name corresponding to the heat conduction equation. Typically
	temp.
fission_rate	Variable name corresponding to the fission rate. Typically fission_rate.

Kernel for the volumetric heat source associated with fission.

# 14.6 BodyForce

```
[./bodyforce]
type = BodyForce
variable = <variable>
value = <real>
function = <string>
[../]
```

type	BodyForce
variable	Variable associated with this volume integral.
value	Constant included in volume integral. Multiplied by the value of function if present.
function	Function to be multiplied by value and used in the volume integral.

Kernel for applying an arbitrary body force to the model.

# 14.7 TimeDerivative

[./timederivative]

```
type = TimeDerivative
variable = <variable>
[../]
```

type TimeDerivative

variable Variable associated with this volume integral.

Kernel for applying a time rate of change term  $(\partial u/\partial t)$  to the model.

# 14.8 Arrhenius Diffusion

```
[./arrheniusdiffusion]
  type = ArrheniusDiffusion
  variable = <variable>
[../]
```

```
type ArrheniusDiffusion
```

variable Variable associated with this volume integral.

Kernel for applying an Arrhenius diffusion term. If present, an ArrheniusDiffusionCoef material model must also be present.

# **15 Materials**

The Materials block is for specifying material properties and models.

```
[Materials]
[./name]
type = <material type>
block = <string list>
...
[../]
[]
```

type Type of material model

block List of blocks. Either block numbers or names.

## **15.1 Thermal Models**

### 15.1.1 HeatConductionMaterial

```
[./heatconductionmaterial]
type = HeatConductionMaterial
thermal_conductivity = <real>
thermal_conductivity_x = <string>
thermal_conductivity_z = <string>
thermal_conductivity_temperature_function = <string>
specific_heat = <real>
specific_heat_temperature_function = <string>
[../]
```

typeHeatConductionMaterialthermal\_conductivityThermal conductivity.thermal\_conductivity\_xThermal conductivity Postprocessor<br/>for the x direction.thermal\_conductivity\_yThermal conductivity Postprocessor<br/>for the y direction.thermal\_conductivity\_zThermal conductivity Postprocessor<br/>for the y direction.thermal\_conductivity\_zThermal conductivity Postprocessor<br/>for the y direction.

thermal_conductivity_temperature_function	Function describing thermal conduc-
	tivity as a function of temperature.
specific_heat	Specific heat.
<pre>specific_heat_temperature_function</pre>	Function describing specific heat as a
	function of temperature.

HeatConductionMaterial is a general-purpose material model for heat conduction. It sets the thermal conductivity and specific heat at integration points.

## 15.1.2 ThermalFuel

```
[./thermalfuel]
type = ThermalFuel
temp = <string>
burnup = <string>
porosity = <string>
initial_porosity = <real> (0.05)
oxy_to_metal_ratio = <real> (2.0)
Pu_content = <real> (0.0)
Gd_content = <real> (0.0)
model = < 0, 1, 2, 3, 4, or 5 for
Duriez, Amaya, Fink-Lucuta, Halden, NFIR, or Modified NFIR >
[../]
```

type	ThermalFuel
temp	Name of temperature variable. Typically temp.
burnup	Name of burnup variable. Typically burnup.
porosity	Name of porosity variable. Typically $\ensuremath{porosity}$ . Optional.
initial_porosity	Initial porosity.
oxy_to_metal_ratio	Ratio of oxygen atoms to metal atoms.
Pu_content	Weight fraction of Pu in MOX fuel (typically 0.07).
Gd_content	Weight fraction of Gd in fuel.

The ThermalFuel model computes specific heat and thermal conductivity for oxide fuel. A number of correlations are available.

## **15.2 Solid Mechanics Models**

#### 15.2.1 CreepPyC

```
[./creeppyc]
type = CreepPyC
```

```
disp_x = <string>
disp_y = <string>
disp_z = <string>
disp_r = <string>
temp = <string>
flux = <string>
density = <real>
youngs_modulus = <real>
poissons_ratio = <real>
thermal_expansion = <real> (0)
stress_free_temperature = <real>
[../]
```

```
CreepPyC
type
                              Variable name for displacement variable in x direction. Typi-
disp_x
                              cally disp_x.
                              Variable name for displacement variable in y direction. Typi-
disp_y
                              cally disp_y.
                              Variable name for displacement variable in z direction. Typi-
disp_z
                              cally disp_z for 3D and disp_y for axisymmetric models.
disp_r
                              Variable name for displacement variable in radial direction
                              for axisymmetric or spherically symmetric cases. Typically
                              disp_x.
                              Name of temperature variable. Typically temp.
temp
                              Variable name corresponding to the fast neutron flux. Typi-
flux
                              cally fast_neutron_flux.
                              The initial material density.
density
                              Coefficient of thermal expansion.
thermal_expansion
stress_free_temperature
                              The stress-free temperature. If not specified, the initial tem-
                              perature is used.
```

CreepPyC is used to model the creep behavior of pyrolytic carbon.

#### 15.2.2 CreepSiC

```
[./creepsic]
type = CreepSiC
disp_x = <string>
disp_y = <string>
disp_z = <string>
disp_r = <string>
temp = <string>
fast_neutron_flux = <string>
```

```
k_function = <string>
youngs_modulus = <real>
poissons_ratio = <real>
thermal_expansion = <real> (0)
stress_free_temperature = <real>
[../]
```

type	CreepSiC
disp_x	Variable name for displacement variable in x direction. Typically disp_x.
disp_y	Variable name for displacement variable in y direction. Typically disp_y.
disp_z	Variable name for displacement variable in z direction. Typically disp_z for 3D and disp_y for axisymmetric models.
disp_r	Variable name for displacement variable in radial direction for axisymmetric or spherically symmetric cases. Typically disp_x.
temp	Name of temperature variable. Typically temp.
fast_neutron_flux	Variable name corresponding to the fast neutron flux. Typically fast_neutron_flux.
k_function	Function that takes temperature as input and gives the K coefficient as output.
youngs_modulus	Young's modulus.
poissons_ratio	Poisson's ratio.
thermal_expansion	Coefficient of thermal expansion.
stress_free_temperature	The stress-free temperature. If not specified, the initial temperature is used.

 ${\tt CreepSiC}$  is used to model the creep behavior of silicon carbide. The relation is

$$\dot{\varepsilon}_{cr} = K \sigma \phi. \tag{15.1}$$

#### 15.2.3 CreepUO2

```
[./creepuo2]
type = CreepUO2
disp_x = <string>
disp_y = <string>
disp_z = <string>
disp_r = <string>
temp = <string>
fission_rate = <string>
```

```
youngs_modulus = <real>
poissons_ratio = <real>
thermal_expansion = <real> (0)
grain_radius = <real> (10e-6)
oxy_to_metal_ratio = <real> (2)
relative_tolerance = <real> (1e-4)
absolute_tolerance = <real> (1e-20)
max_its = <integer> (10)
output_iteration_info = <true or false> (false)
stress_free_temperature = <real>
matpro_youngs_modulus = <true or false> (false)
matpro_poissons_ratio = <true or false> (false)
matpro_thermal_expansion = <true or false> (false)
burnup = <string>
[../]
```

type	CreepU02
disp_x	Variable name for displacement variable in x direction. Typically disp_x.
disp_y	Variable name for displacement variable in y direction. Typically disp_y.
disp_z	Variable name for displacement variable in z direction. Typ- ically disp_z for 3D and disp_y for axisymmetric models.
disp_r	Variable name for displacement variable in radial direction for axisymmetric or spherically symmetric cases. Typically disp_x.
temp	Name of temperature variable. Typically temp.
fission_rate	Variable name corresponding to the fission rate. Typically fission_rate.
youngs_modulus	Young's modulus.
poissons_ratio	Poisson's ratio.
thermal_expansion	Coefficient of thermal expansion.
grain_radius	Fuel grain radius.
oxy_to_metal_ratio	Oxygen to metal ratio.
relative_tolerance	Relative convergence tolerance for material model iterations.
absolute_tolerance	Absolute convergence tolerance for material model iterations.
max_its	Maximum number of material model convergence iterations.
output_iteration_info	Whether to output material model convergence information.
stress_free_temperature	The stress-free temperature. If not specified, the initial temperature is used.

matpro_youngs_modulus	Set to true to use correlations for Young's modulus from MATPRO [8].
matpro_poissons_ratio	Set to true to use correlations for Poisson's modulus from MATPRO [8].
<pre>matpro_thermal_expansion</pre>	Set to true to use correlations for coefficient of thermal expansion from MATPRO [8].
burnup	Name of burnup variable. Only required if using MATPRO correlations. Typically burnup.

The CreepU02 is used to model the creep behavior of  $UO_2$ .

#### 15.2.4 Elastic

```
[./elastic]
type = Elastic
disp_x = <string>
disp_y = <string>
disp_z = <string>
disp_r = <string>
temp = <string>
youngs_modulus = <real>
poissons_ratio = <real>
thermal_expansion = <real> (0)
stress_free_temperature = <real>
[../]
```

type	Elastic
disp_x	Variable name for displacement variable in x direction. Typi-
	cally disp_x.
disp_y	Variable name for displacement variable in y direction. Typi-
	cally disp_y.
disp_z	Variable name for displacement variable in z direction. Typi-
	cally disp_z for 3D and disp_y for axisymmetric models.
disp_r	Variable name for displacement variable in radial direction
	for axisymmetric or spherically symmetric cases. Typically
	disp_x.
temp	Name of temperature variable. Typically temp.
youngs_modulus	Young's modulus.
poissons_ratio	Poisson's ratio.
thermal_expansion	Coefficient of thermal expansion.
stress_free_temperature	The stress-free temperature. If not specified, the initial tem-
	perature is used.

The Elastic model is a simple hypo-elastic model.

#### 15.2.5 IrradiationGrowthZr4

```
[./irradiationgrowthzr4]
type = IrradiationGrowthZr4
fast_neutron_fluence = <string>
Ag = <real> (3e-20)
ng = <real> (0.794)
[../]
```

type	IrradiationGrowthZr4						
fast_neutron_fluence	Name	of	fast	neutron	fluence	variable.	Typically
	fast_neutron_fluence.						
Ag	Materia	l cor	istant t	hat depend	ls on the c	ladding me	talurgical state.
ng	Materia	l cor	istant t	hat depend	ls on the c	ladding me	talurgical state.

The IrradiationGrowthZr4 model incorporates anisotropic volumetric swelling to track axial elongation in Zr4 cladding.

#### 15.2.6 PyCIrradiationStrain

```
[./pycirradiationstrain]
type = PyCIrradiationStrain
fluence = <string>
pyc_type = <string> (buffer)
[../]
```

```
type PyCIrradiationrStrain
```

```
fluence Variable name corresponding to the fast neutron fluence. Typically fast_neutron_fluence.
```

pyc\_type One of buffer or dense.

The PyCIrradiationStrain model tracks the irradiation-induced strain in pyrolytic carbon. The strain is isotropic for the buffer type and differs in the radial and tangential directions for the dense type.

### 15.2.7 MechZry

```
[./mechzry]
type = MechZry
fast_neutron_flux = <string>
fast_neutron_fluence = <string>
```

```
initial_fast_fluence = <real> (0.0)
 cold_work_factor = <real> (0.01)
 oxygen_concentration = <real> (0.0)
 relative_tolerance = <real> (1e-4)
 absolute_tolerance = <real> (1e-20)
 max_its = <integer> (10)
 output_iteration_info = <bool> (false)
 model_irradiation_growth = <bool> (true)
 model_primary_creep = <bool> (true)
 model_thermal_creep = <bool> (true)
 model_irradiation_growth = <bool> (true)
 model_thermal_expansion = <bool> (true)
 model_elastic_modulus = <bool> (false)
 stress_free_temperature = <real>
 material_type = < 0 or 1 for SRA or RXA >
[../]
```

type	MechZry				
fast_neutron_flux	Variable name corresponding to the fast neutron flux. Typically fast_neutron_flux.				
fast_neutron_fluence	Name of fast neutron fluence variable. Typically fast_neutron_fluence.				
initial_fast_fluence	The initial fast neutron fluence.				
cold_work_factor	Cold work factor.				
oxygen_concentration	Oxygen concentration in ppm.				
relative_tolerance	Relative convergence tolerance for material model iterations.				
absolute_tolerance	Absolute convergence tolerance for material model itera-				
	tions.				
max_its	Maximum number of material model convergence iterations.				
output_iteration_info	Whether to output material model convergence information.				
model_irradiation_creep	Whether to model irradiation-induced creep.				
model_primary_creep	Whether to model primary creep.				
model_thermal_creep	Whether to model steady state thermal creep.				
model_irradiation_growth	Whether to model irradiation growth.				
model_thermal_expansion	Whether to use MATPRO model for thermal expansion.				
model_elastic_modulus	Whether to calculate temperature-dependent elastic moduli.				
stress_free_temperature	The stress-free temperature. If not specified, the initial temperature is used.				
material_type	Cladding material type. 0 for SRA, 1 for RXA.				

The MechZry model includes the option to model primary, thermal, and irradiation-induced creep. It is also possible to turn on irradiation growth. If irradiation growth is turned on, do not

include the IrradiationGrowthZr4 model.

#### 15.2.8 RelocationUO2

```
[./relocationuo2]
type = RelocationU02
burnup = <string>
diameter = <real>
q = <string>
gap = <real>
burnup_relocation_stop = <real>
relocation_activation1 = <real> (19685.039)
relocation_activation2 = <real> (45931.759)
relocation_activation3 = <real> (32808.399)
axial_axis = <0, 1, or 2 for x, y, or z>
[../]
```

type	RelocationUO2		
burnup	Name of burnup variable. Typically burnup.		
diameter	As fabricated cold diameter of pellet in meters.		
q	Linear heat rate in pellet in W/m.		
gap	As fabricated cold diametral gap in m.		
burnup_relocation_stop	Burnup at which relocation strain stops in FIMA.		
relocation_activation1	First activation linear power in W/m. The linear power at which relocation turns on.		
relocation_activation2	Second activation linear power in W/m. The linear power at which relocation transitions from the initial regime to the secondary regime.		
relocation_activation3	Third activation linear power in W/m. The linear power offset in the secondary regime.		
axial_axis	Coordinate axis of the axial direction of the fuel stack.		

The RelocationU02 model accounts for cracking and relocation of fuel pellet fragments in the radial direction. This model is necessary for accurate modeling of LWR fuel.

#### 15.2.9 ThermallrradiationCreepZr4

```
[./thermalirradiationcreepzr4]
type = ThermalIrradiationCreepZr4
disp_x = <string>
disp_y = <string>
disp_z = <string>
disp_r = <string>
```

```
temp = <string>
 a\_coeff = <real > (3.14e24)
 n_exponent = < real > (5)
 activation_energy = <real> (2.7e5)
 gas_constant = \langle real \rangle (8.3143)
 fast_neutron_flux = <string>
 c0_coef = <real> (9.881e-28)
 c1\_coef = <real > (0.85)
 c2\_coef = <real > (1)
 youngs_modulus = <real>
 poissons_ratio = <real>
 thermal_expansion = <real> (0)
 relative_tolerance = <real> (1e-4)
 absolute_tolerance = <real> (1e-20)
 max_its = <integer> (10)
 output_iteration_info = <true or false> (false)
 stress_free_temperature = <real>
[../]
```

ThermalIrradiationCreepZr4
Variable name for displacement variable in x direction. Typi-
cally disp_x.
Variable name for displacement variable in y direction. Typi-
cally disp_y.
Variable name for displacement variable in z direction. Typi-
cally disp_z for 3D and disp_y for axisymmetric models.
Variable name for displacement variable in radial direction
for axisymmetric or spherically symmetric cases. Typically
disp_x.
Name of temperature variable. Typically temp.
The leading coefficient in the thermal creep term.
The exponent in the thermal creep term.
The activation energy.
The universal gas constant.
Variable name corresponding to the fast neutron flux. Typi-
cally fast_neutron_flux.
The leading coefficient in the irradiation creep term.
The exponent on the irradiation creep fast neutron flux term.
The exponent on the irradiation creep stress term.
Young's modulus.
Poisson's ratio.
Coefficient of thermal expansion.

relative_tolerance	Relative convergence tolerance for material model iterations.
absolute_tolerance	Absolute convergence tolerance for material model iterations.
max_its	Maximum number of material model convergence iterations.
output_iteration_info	Whether to output material model convergence information.
stress_free_temperature	The stress-free temperature. If not specified, the initial temperature is used.
burnup	Name of burnup variable. Typically burnup.

The ThermalIrradiationCreepZr4 is used for Zr4 cladding in LWR simulations. It includes fits for the temperature, irradiation, and stress effects on cladding creep.

#### 15.2.10 VSwellingUO2

```
[./vswellinguo2]
type = VSwellingU02
temp = <string>
burnup = <string>
density = <real>
total_densification = <real> (0.01)
complete_burnup = <real> (5)
[../]
```

type	VSwellingUO2
temp	Name of temperature variable. Typically temp.
burnup	Name of burnup variable. Typically burnup.
density	Initial fuel density.
total_densification	The densification that will occur given as a fraction of theoretical density.
complete_burnup	The burnup at which densification is complete (MWd/kgU).

The VSwellingUO2 model computes a volumetric strain to account for solid and gaseous swelling and for densification.

## 15.3 Fission Gas Models

Fission gas production and release modeling plays a vital role in fuel performance analysis. Fission gas affects swelling, porosity, thermal conductivity, gap conductivity, and rod internal pressure. The Sifgrs model is recommended.

### 15.3.1 ForMas

```
[./formas]
 type = ForMas
 grain_radius = <real> (10e-6)
 resolution_rate = <real> (1e-7)
 resolution_depth = <real> (1e-8)
 bubble_radius = <real> (5e-7)
 bubble_shape_factor = <real> (0.287)
 surface_tension = <real> (0.626)
 fractional_coverage = <real> (0.5)
 external_pressure = <real> (10e6)
 plenum_pressure = <string>
 external_pressure_function = <string>
 release_fraction = <real> (0)
 fractional_yield = <real> (0.3017)
 calibration_factor = <real> (1)
[../]
```

type	ForMas
grain_radius	Initial fuel grain radius.
resolution_rate	Resolution rate from intergranular bubbles (1/s).
resolution_depth	Resolution layer depth.
bubble_radius	Grain boundary bubble radius.
bubble_shape_factor	Non-spherical bubble shape factor.
surface_tension	Bubble surface tension (J/m <sup>2</sup> ).
fractional_coverage	Fractional coverage of grain boundary at saturation.
external_pressure	Constant external hydrostatic pressure.
plenum_pressure	The name of the plenum pressure Postprocessor.
external_pressure_function	Function describing the external pressure.
release_fraction	Fraction of boundary and resolved gas released at satura-
	tion.
fractional_yield	Fractional yield of fission gas atoms per fission.
calibration_factor	Calibration factor to be multiplied by gas saturation den- sity.

The ForMas model is maintained but not actively developed. The Sifgrs model is recommended.

#### 15.3.2 Sifgrs

```
[./sifgrs]
type = Sifgrs
initial_grain_radius = <real> (5e-6)
```

```
hydrostatic_stress_const = <real> (0.0)
 surface_tension = < real > (0.5)
 saturation_coverage = <real> (0.5)
 hbs_release_burnup = <real> (100)
 initial_porosity = <real> (0.05)
 density = <real>
 solid_swelling_factor = <real> (5.577e-5)
 total_densification = <real> (0.01)
 end_densification_burnup = <real> (5)
 pellet_brittle_zone = <string>
 diff_coeff_option <integer>
 compute_swelling = <bool> (false)
 ath_model = <bool> (false)
 gbs_model = <bool> (false)
 ramp_model = <bool> (false)
 hbs_model = <bool> (false)
 file_name = <string>
 format = <string> (rows)
 rod_ave_lin_power = <string>
 axial_power_profile = <string>
 grain_radius = <string>
 pellet_id = <string>
 temp = <string>
 fission_rate = <string>
 hydrostatic_stress = <string>
 burnup = <string>
[../]
```

type	Sifgrs
initial_grain_radius	Initial grain radius.
hydrostatic_stress_const	A constant value for hydrostatic stress. Ignored if hydrostatic_stress is given.
surface_tension	Bubble surface tension (J/m <sup>2</sup> ).
saturation_coverage	Fractional grain boundary bubble coverage at saturation.
hbs_release_burnup	Threshold local burnup for gas release from the HBS porosity (MWd/kgU).
initial_porosity	Initial fuel porosity.
density	Initial fuel density.
solid_swelling_factor	Solid swelling coefficient.
total_densification	The densification that will occur given as a fraction of theo- retical density.
end_densification_burnup	The burnup at which densification is complete (MWD/kgU).
pellet_brittle_zone	The name of the UserObject that computes the width of the brittle zone.

diff_coeff_option	One of 0 (Turnbull), 1 (Andersson, low burnup), 2 (Andersson, high burnup), or 3 (Turnbull modified).			
compute_swelling	Whether to compute fuel swelling.			
ath_model	Whether to compute athermal gas release.			
gbs_model	Whether to compute grain boundary sweeping.			
ramp_model	Whether to include the ramp release model. Requires file_name.			
hbs_model	Whether to include high burnup structure gas release.			
file_name	File describing rod averaged linear power. This power is the total power, the power from the volumetric fission rate times the volume of fuel times the energy per fission.			
format	One of rows or columns.			
rod_ave_lin_pow	Function describing rod averaged linear power. This power is the total power, the power from the volumetric fission rate times the volume of fuel times the energy per fission.			
axial_power_profile	Function describing axial power profile.			
grain_radius	Variable name for grain radius.			
pellet_id	Variable name for pellet id. Typically pellet_id.			
temp	Variable name for temperature variable. Typically temp.			
fission_rate	Variable name corresponding to the fission rate. Typically fission_rate.			
hydrostatic_stress	Variable name for hydrostatic stress. Typically hydrostatic_stress.			
burnup	Name of burnup variable. Typically burnup.			

Sifgrs is the recommended fission gas model.

# 15.4 Mass Diffusion Models

```
[./arrheniusdiffusioncoef]
type = ArrheniusDiffusionCoef
d1 = <real> (5.6e-8)
d1_function = <string>
d1_function_variable = <string>
d2 = <real> (5.2e-4)
q1 = <real> (2.09e5)
q2 = <real> (3.62e5)
gas_constant = <real> (8.3143)
temp = <string>
[../]
```

type	ArrheniusDiffusionCoef
d1	First coefficient $(m^2/2)$ .
dl_function	Function to be multiplied by d1.
dl_function_variable	Variable to be used when evaluating dl_function. If not given, time will be used.
d2	Second coefficient $(m^2/2)$ .
q1	First activation energy (J/mol).
q2	Second activation energy (J/mol).
gas_constant	Universal gas constant (J/mol/K).
temp	Name of temperature variable. Typically temp.

This material computes a two-term Arrhenius diffusion coefficient of the form

$$d = d_1 \exp\left(\frac{-q_1}{RT}\right) + d_2 \exp\left(\frac{-q_2}{RT}\right).$$
(15.2)

## 15.5 Other Models

### 15.5.1 Density

```
[./density]
type = Density
disp_x = <string>
disp_y = <string>
disp_z = <string>
disp_r = <string>
density = <real>
[../]
```

type	Density
disp_x	Variable name for displacement variable in x direction. Typically disp_x.
disp_y	Variable name for displacement variable in y direction. Typically disp_y.
disp_z	Variable name for displacement variable in z direction. Typically $disp_z$ for 3D and $disp_y$ for axisymmetric models.
disp_r	Variable name for displacement variable in radial direction for axisymmetric or spherically symmetric cases. Typically disp_x.
density	Density.

The Density model creates a material property named density. If coupled to displacement variables, the model adjusts density based on deformation.

# **16 Postprocessors**

MOOSE Postprocessors compute a single scalar value at each timestep. These can be minimums, maximums, averages, volumes, or any other scalar quantity. One example of the use of Postprocessors in BISON is computing the gas volume of an LWR rod. The gas volume changes timestep to timestep, but since it is a single scalar quantity, a Postprocessor computes this value.

```
[Postprocessors]
[./name]
type = <postprocessor type>
block = <string list>
boundary = <string list>
output = <string>
...
[../]
```

type	Type of postprocessor
block	List of blocks. Either block numbers or names.
boundary	List of boundaries (side sets). Either boundary numbers or names.
output	The options are: none, screen, file, both, auto (no output, output to screen only, output to files only, output both to screen and files, same as both but no warnings if output options conflict).

All Postprocessors act on either boundaries or blocks. If no block or boundary is specified, the Postprocessor will act on the entire model.

## 16.1 SideAverageValue

```
[./sideaveragevalue}
type = SideAverageValue
variable = <string>
[../]
```

typeSideAverageValuevariableThe variable this Postprocessor acts on.

SideAverageValue computes the area- or volume-weighted average of the named variable. It may be used, for example, to calculate the average temperature over a side set.

## 16.2 InternalVolume

```
[./internalvolume}
type = InternalVolume
scale_factor = <real> (1)
addition = <addition> (0)
[../]
```

type	InternalVolume	
scale_factor	Scale factor to be applied to the internal volume calcu	lation.
addition	Number to be added to internal volume calculation. scaled.	This addition is not

InternalVolume computes the volume of an enclosed space. The entire boundary of the enclosed space must be represented by the given side set. If the given side set points outward, InternalVolume will report a negative volume.

## 16.3 Reporter

```
[./reporter]
  type = Reporter
  default = <real> (0)
[../]
```

type Reporter

default Default or initial value of the Postprocessor.

Reporter is a unique Postprocessor in that it does not calculate anything at all. It is simply a scalar value that can be set and used by other MOOSE objects. It is commonly used to report scalar quantities computed by boundary conditions, kernels, and other objects.

## 16.4 TimestepSize

[./dt]
type = TimestepSize
[../]

type TimestepSize

TimestepSize reports the timestep size.

## 16.5 NumNonlinearIterations

```
[./numnonlineariters]
  type = NumNonlinearIterations
[../]
```

#### type NumNonlinearIterations

NumNonlinearIterations reports the number of nonlinear iterations in the just-completed solve.

# 16.6 PlotFunction

```
[./plotfunction]
  type = PlotFunction
  function = <string>
  scale_factor = <real> (1)
[../]
```

type	PlotFunction
function	The function to evaluate.
scale_factor	Scale factor to be applied to the function value.

PlotFunction gives the value of the supplied function at the current time, optionally scaled with scale\_factor.

## 16.7 ElementIntegralPower

```
[./elementintegralpower]
type = ElementIntegralPower
fission_rate = <string>
energy_per_fission = <real> (3.28451e-11)
[../]
```

type	Element	Integr	calPower					
fission_rate	Variable	name	corresponding	to	the	fission	rate.	Typically
	fission	_rate.						

energy\_per\_fission The energy released per fission in J/fission.

ElementIntegralPower computes the power in the supplied block given the fission rate variable and energy per fission.

# 16.8 SideFluxIntegral

```
[./sidefluxintegral]
type = SideFluxIntegral
variable = <string>
diffusivity = <string>
[../]
```

type	SideFluxIntegral
variable	Variable to be used in the flux calculation.
diffusivity	The diffusivity material property to be used in the calculation.

SideFluxIntegral computes the integral of the flux over the given boundary.

# **17 Executioner**

The Executioner block describes how the simulation will be executed. It includes commands to control the solver behavior and time stepping.

```
[Executioner]
 type = <string>
 solve_type = <string>
 print_linear_residuals = <bool> (false)
 petsc_options = <string list>
 petsc_options_iname = <string list>
 petsc_options_value = <string list>
 line_search = <string>
 l_max_its = <integer>
 l_tol = <real>
 nl_max_its = <integer>
 nl_rel_tol = <real>
 nl_abs_tol = <real>
 start_time = <real>
 dt = <real>
 end_time = <real>
 num_steps = <integer>
 dtmax = <real>
 dtmin = <real>
 optimal_iterations = <integer>
 iteration_window = <integer> (0.2*optimal_iterations)
 linear_iteration_ratio = <integer> (25)
```

```
Several available. Typically AdaptiveTransient.
type
                           One of PJFNK (preconditioned JFNK), JFNK (JFNK),
solve_type
                           NEWTON (Newton), or SolveFD (Jacobian computed by finite
                           difference-serial only, slow).
print_linear_residuals
                           Whether to print linear residuals to the screen.
                           PETSc flags.
petsc_options
                           Names of PETSc name/value pairs.
petsc_options_iname
                           Values of PETSc name/value pairs.
petsc_options_value
line_search
                           Line search type. Typically none.
                           Maximum number of linear iterations per solve.
l_max_its
l_tol
                           Linear solve tolerance.
                           Maximum number of nonlinear iterations per solve.
nl_max_its
```

nl_rel_tol	Nonlinear relative tolerance.				
nl_rel_abs	Nonlinear absolute tolerance.				
start_time	The start time of the analysis.				
dt	The initial timestep size.				
end_time	The end time of the analysis.				
num_steps	The maximum number of time steps.				
dtmax	The maximum allowed timestep size. Used with AdaptiveTransient.				
dtmin	The minimum allowed timestep size. Used with AdaptiveTransient.				
optimal_iterations	The target number of nonlinear iterations for adaptive timestepping. Used with AdaptiveTransient.				
iteration_window	The size of the nonlinear iteration window for adaptive timestepping. Used with AdaptiveTransient.				
linear_iteration_ratio	The ratio of linear to nonlinear iterations to determine target linear iterations and window for adaptive timestepping.				

Many Executioner types exist. For each type, specific options are available. To see the complete set of possibilities, follow the Input Syntax link on the BISON wiki page.

Similarly, many PETSc options exist. Please see the online PETSc documentation for details. Given the many possibilities in the Executioner block, it may be helpful to review examples in the BISON tests, examples, and assessment directories.

# 18 Output

```
[Output]
file_base = <string> (mesh file base name + `_out')
interval = <integer> (1)
exodus = <bool> (false)
max_pps_rows_screen = <integer> (15)
postprocessor_csv = <bool> (false)
output_initial = <bool> (false)
[../]
```

file_base	Base file name for output files.
interval	The interval at which solutions are written to the output files.
exodus	Specifies that you would like ExodusII solution files. Typically set
	to true.
<pre>max_pps_rows_screen</pre>	The maximum number of postprocessor values displayed on screen
	during a timestep (set to 0 for unlimited).
postprocessor_csv	Specifies whether you would like a csv file containing
	Postprocessor values.
output_initial	Specifies whether you would like the initial state of the model writ-
	ten to the output file. Typically set to true.

The Output block lists parameters that control the frequency and type of results files produced.

# **19 Dampers**

Dampers are used to decrease the attempted change to the solution with each nonlinear step. This can be useful in preventing the solver from changing the solution dramatically from one step to the next. This may prevent, for example, the solver from attempting to evaluate negative temperatures.

The MaxIncrement damper is commonly used.

# **19.1 MaxIncrement**

```
[Dampers]
[./maxincrement]
type = MaxIncrement
max_increment = <real>
variable = <string>
[../]
```

type	MaxIncrement
max_increment	The maximum change in solution variable allowed from one nonlinear step
	to the next.
variable	Variable that will not be allowed to change beyond max_increment from nonlinear step to nonlinear step.

The MaxIncrement damper limits the change of a variable from one nonlinear step to the next.

# 20 UserObjects

# 20.1 PelletBrittleZone

```
[./pelletbrittlezone]
type = PelletBrittleZone
pellet_id = <string>
temp = <string>
pellet_radius = <real>
a_lower = <real>
a_upper = <real>
number_pellets = <integer>
[../]
```

type	PelletBrittleZone
pellet_id	Variable name for pellet id. Typically pellet_id.
temp	Name of temperature variable. Typically temp.
pellet_radius	The outer radius of the fuel.
a_lower	The lower axial coordinate of the fuel stack.
a_upper	The upper axial coordinate of the fuel stack.
number_pellets	Number of fuel pellets.

PelletBrittleZone computes the brittle zone width on a per-pellet basis.

# 21 Timestepping

The time steps taken by BISON can be specified directly by providing either a single fixed time step to take throughout the analysis, or by providing the time step as a function of time. Alternatively, an adaptive timestepping algorithm can be used to modify the time step based on the difficulty of the iterative solution, as quantified by the numbers of linear and nonlinear iterations required to drive the residual below the tolerance required for convergence.

All of these types of timestepping can be obtained by using the AdaptiveTransient type of executioner. The parameters used in this executioner to obtain these different types of time stepping are described below.

### 21.1 Direct Time Step Control with Constant Time Step

The most basic way to control the time steps taken by BISON is to use the AdaptiveTransient executioner with options that instruct it to take a single, fixed time step over the duration of the analysis. To take time steps in this way, simply specify the time step to be taken using the dt parameter.

While using a constant time step, if the solver fails to obtain a converged solution for a given step, the executioner cuts back the step size and attempts to advance the time from the previous step using a smaller time step. The time step is cut back by multiplying the time step by the factor specified by the user through the cutback\_factor parameter.

If the solution with the cut-back time step is still un-successful, it is repeatedly cut back until a successful solution is obtained. The user can optionally specify a minimum time step through the dtmin parameter. If the time step must be cut back below the minimum size without obtaining a solution, BISON exits with an error.

If the time step has been cut back to obtain a solution, BISON uses that cut-back time step in the next step. If that solution is successful, BISON attempts to increase the time step by multiplying it by the value specified by the growth\_factor parameter. This is done repeatedly until the time step has grown back to the original value specified in the dt parameter.

## 21.2 Direct Time Step Control with Varying Time Step Size

BISON can optionally take time steps that are specified by the user, but which can vary over time. This is accomplished by providing a set of pairs of times and time steps instead of with a single fixed time step. A vector of time steps is provided using the time\_dt parameter. An accompanying vector of corresponding times is specified using the time\_t parameter. These two vectors are used to form a time step vs. time function. The time step for a given step is computed by linearly interpolating between the pairs of values provided in the vectors. The same procedure that is used with a fixed time step is used to cut back the time step from the user-specified value if a failed solution occurs. The time step is grown until it reaches to the value specified by the time-dependent function in the same way that is done with a fixed time step.

### 21.3 Adaptive Time Stepping

The two methods for user-specified time stepping described above can be used to cut the time step back if a solution fails. While this technique can be helpful to get past difficult parts of the time history, it can be much more efficient to adapt the time step based on the difficulty of the solution.

The AdaptiveTransient executioner provides an option to grow or shrink the time step based on the number of iterations taken to obtain a converged solution in the last converged step. The adaptive time stepping option is activated by setting a value for the optimal\_iterations parameter. This parameter is the number of nonlinear iterations per time step that provides optimal solution efficiency. If more iterations than that are required, the time step may be too large, resulting in undue solution difficulty, while if fewer iterations are required, it may be possible to take larger time steps to obtain a solution more quickly.

A second parameter, iteration\_window, is used to control the size of the region in which the time step is held constant. As shown in Figure 21.1, if the number of nonlinear iterations for convergence is lower than (optimal\_iterations-iteration\_window), the time step is increased, while if more than (optimal\_iterations+iteration\_window), iterations are required, the time step is decreased. The iteration\_window parameter is optional. If it is not specified, it defaults to 1/5 the value specified for optimal\_iterations.

The decision on whether to grow or shrink the time step is based both on the number of nonlinear iterations and the number of linear iterations. The parameters mentioned above are used to control the optimal iterations and window for nonlinear iterations. The same criterion is applied to the linear iterations. Another parameter, linear\_iteration\_ratio, which defaults to 25, is used to control the optimal iterations and window for the linear iterations. These are calculated by multiplying linear\_iteration\_ratio by optimal\_iterations and iteration\_window, respectively.

To grow the time step, the growth criterion must be met for both the linear iterations and nonlinear iterations. If the time step shrinkage criterion is reached for either the linear or nonlinear iterations, the time step is decreased. To control the time step size only based on the number of nonlinear iterations, set linear\_iteration\_ratio to a large number.

If the time step is to be increased or decreased, that is done using the factors specified with the growth\_factor and cutback\_factor, respectively. If a solution fails to converge when adaptive time stepping is active, a new attempt is made using a smaller time step in the same manner as with the fixed time step methods. The maximum and minimum time steps can be optionally specified using the dtmax and dtmin parameters, respectively.


Figure 21.1: Criteria used to determine adaptive time step size

# 22 Mesh Script

# 22.1 Overview

To ease generation of LWR fuel meshes, a mesh script is available. The script relies on CU-BIT [6].

#### 22.1.1 Run the Main Script

The mesh script is at bison/tools/U02/. The main script (mesh\_script.sh) is run from the shell command line. This script invokes the Python meshing script (mesh\_script.py) and passes it an input file named mesh\_script\_input.py by default.

You invoke the script as:

```
> ./mesh_script.sh [-c -d -l] [-p path to mesh_script.py] [-i
mesh_script_input.py]
```

The -c flag will cause the script to check whether CUBIT can be loaded. The -d flag results in the deletion of the CUBIT journal file when the script completes. The -1 flag will generate a log file (otherwise messages will go to the terminal). The -p flag, which is rarely used, tells the script where to find the mesh\_script.py file. Finally, you may supply any mesh script input file with the -i flag.

The main script generates an exodus file, with QUAD elements in 2D and HEX elements in 3D.

#### 22.1.2 Mesh Architecture

Figure 22.1 provides an overview of the architecture of a fuel rod. A fuel rod is composed of a clad, a stack of pellets, and optionally a liner extruded on the inner surface of the clad. Each component of this architecture corresponds to a different block in the BISON input and mesh files. In the mesh input file, you refer to each block through a specific dictionary to create it. In the Exodus file, blocks are numbered, and a name is provided for each of them.

The pellets contained in a fuel rod can have different geometries. There is a block for each geometry, in the input file as well as in the Exodus file.

# 22.2 Input File Review

## 22.2.1 Pellet Type

This dictionary encapsulates a pellet geometry and the quantity of the corresponding pellets. To refer to a parameter, you have to know its key (the quoted string between brackets).





Figure 22.1: Overview of the architecture of a fuel rod.

```
# Pellet Type 1
Pellet1= {}
Pellet1['type'] = 'discrete'
Pellet1['quantity'] = 5
Pellet1['mesh_density'] = 'medium'
Pellet1['outer_radius'] = 0.0041
Pellet1['inner_radius'] = 0
Pellet1['height'] = 2*5.93e-3
Pellet1['dish_spherical_radius'] = 1.01542e-2
Pellet1['dish_depth'] = 3e-4
Pellet1['chamfer_width'] = 5.0e-4
Pellet1['chamfer_height'] = 1.6e-4
```

- 'type' Type *string*. Must be 'discrete' or 'smeared'. From a geometric point of view, a smeared pellet is a rectangle. Two consecutive smeared pellets have their top and bottom surfaces merged.
- 'quantity' Type int. Number of pellets created with this geometry.
- 'mesh\_density' Type string.
- 'outer\_radius' Type float. Outer radius of the pellet.
- 'inner\_radius' Type float. Inner radius of the pellet.
- 'height' Type float. Pellet height.
- 'dish\_spherical\_radius' Type *float*. Spherical radius of the dishing. Needed only if type is 'discrete'.
- 'dish\_depth' Type float. Depth of the dishing. Needed only if type is 'discrete'.
- 'chamfer\_width' Type *float*. Radial chamfer length in RZ coordinates. Must be zero for a non-chamfered pellet. Needed only if type is 'discrete'.
- 'chamfer\_height' Type *float*. Axial chamfer length in RZ coordinates. Must be zero for a non-chamfered pellet. Needed only if type is 'discrete'. If either chamfer\_width or chamfer\_height is zero, both must be zero.

### 22.2.2 Pellet Collection

```
pellets = [Pellet1, Pellet2, Pellet3]
```

This is a list of the pellets that make up the pellet stack. The geometries are ordered from the bottom to the top of the stack. A pellet type block must be present in this list to be created.

#### 22.2.3 Stack Options

```
# Stack options
pellet_stack = {}
pellet_stack['merge_pellets'] = True
pellet_stack['higher_order'] = False
pellet_stack['angle'] = 0
```

- 'merge\_pellets' Type *string*. Control type of merging between pellets. Options are: 'yes', 'no', 'point', 'surface'. See Table 22.1 for a complete description. Note that any other string results in pellets that are not merged.
- 'higher\_order' Type boolean. Control order of mesh elements. See Table 22.2
- 'angle' Type *int*. Between 0 and 360. Angle of revolution of the pellet stack. If 0, creates a 2D fuel rod. If greater than 0, creates a 3D fuel rod.

	2D discrete	2D smeared	3D discrete
'yes'	vertex	curve	curve
'no'	not merged	not merged	not merged
'point'	vertex	vertex	curve
'surface'	not merged	curve	not merged

Table 22.1: Merging control. 'Vertex' means that the pellets are merged at their common vertex which is the closest from the centerline. In 2D, 'curve' means that the pellets are merged at their common curve. In 3D, 'curve' means that the pellets are merged at the curve generated by the corresponding merged vertex in 2D rz geometry.

	False	True
2D	QUAD4	QUAD8
3D	HEX8	HEX20

Table 22.2: Order of generated elements

## 22.2.4 Clad

```
clad = {}
clad['mesh_density'] = 'medium'
clad['gap_width'] = 8e-5
clad['bot_gap_height'] = 1e-3
clad['clad_thickness'] = 5.6e-4
clad['top_bot_clad_height'] = 2.24e-3
```

```
clad['plenum_fuel_ratio'] = 0.045
clad['with_liner'] = False
clad['liner_width'] = 5e-5
```

- 'mesh\_density' Type *string*. CAUTION: the mesh density of the clad is related to the mesh density of the pellets which use the *same* mesh dictionary as the clad.
- 'gap\_width' Type *float*. Radial width of the gap between the fuel and the clad (or the liner).
- 'bot\_gap\_height' Type float. Axial height between fuel and top/bottom of the gap.
- 'clad\_thickness' Type float. Thickness of the sleeve of the clad.
- 'top\_bot\_clad\_height' Type float. Height of the bottom and of the top of the clad.
- 'plenum\_fuel\_ratio' Type float. Ratio of the free volume by the volume of the fuel.
- 'with\_liner' Type boolean. Whether to include a liner.
- 'liner\_width' Type float. Liner width.

#### 22.2.5 Meshing Parameters

```
# Parameters of mesh density 'coarse'
coarse = {}
coarse['pellet_r_interval'] = 6
coarse['pellet_dish_interval'] = 2
coarse['pellet_flat_top_interval'] = 3
coarse['pellet_chamfer_interval'] = 1
coarse['pellet_slices_interval'] = 4
coarse['clad_radial_interval'] = 3
coarse['clad_sleeve_scale_factor'] = 4
coarse['cap_radial_interval'] = 6
coarse['cap_vertical_interval'] = 3
coarse['pellet_angular_interval'] = 6
coarse['clad_angular_interval'] = 12
```

The user defines a dictionary containing the mesh parameters. The user can specify the name of this dictionary as long as the name is consistent with the names defined in the pellet type blocks for mesh\_density. pellet\_r\_interval and pellet\_z\_interval are used only with smeared pellet meshes. Figure 22.2 explains other parameters.

The angular intervals are for 3D geometries and correspond to the created arcs of circle. Note that to have a nice mesh, you may want to have the same number of interval on the diameter of the fuel rod and on this arc of circle.





(a) Pellet. Dashed lines represent RZ axes.

(b) Clad. Represented in RZ.

# 22.3 Output File Review



Figure 22.1 summarizes names and number of the blocks in the exodus file. Figure 22.3 summarizes the numbering for the sidesets and nodesets.

Figure 22.3: Sidesets, nodesets and blocks ids in the exodus file

# 22.4 Things to Know

#### 22.4.1 Main Script

The main script is written in python v2.5. It is organized in classes: Pellet, PelletStack, Clad, Liner and FuelRod. The link between the input file and the main is assured by three functions. A first function is charged to pick read the input file. A second function checks that the syntax of the input file makes sense for the main script. The third function creates the mesh based on the input file.

#### 22.4.2 Error Messages

AttributeError Caused by a missing class in the input file.

**KeyError** Often is caused by a wrong key in the input file. The main script should check that the keys entered in the input file are valid and specify which key is not valid if it occurs.

Other errors should be accompanied by a descriptive message. Contact the developers if the error message is not helpful.

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